

## Solution

### ALTERNATING CURRENT WS 1

#### Class 12 - Physics

1.

(c) step-up transformer with turn ratio 1 : 2

**Explanation:** As,  $\frac{N_p}{N_s} = \frac{V_p}{V_s}$  ( $= \frac{\text{input}}{\text{output}}$ )

Thus,  $\frac{N_p}{N_s} = \frac{110}{220} = \frac{1}{2}$

As,  $N_p < N_s$ , hence it is a step-up transformer.

2.

(a)  $\omega^2 LC$

**Explanation:**  $\omega^2 LC$

3.

(c) Zero

**Explanation:** Power =  $V_{\text{rms}} \times I_{\text{rms}} \times \cos \phi$

Here

$\phi = \frac{\pi}{2}$  So,

Power = 0

4.

(b) 127  $\mu\text{F}$

**Explanation:** Voltage and current will be in phase when  $X_C = X_L$

Or,  $\frac{1}{\omega C} = \omega L$

Or,  $\frac{1}{2\pi f C} = 2\pi f L$

Or,  $C = \frac{1}{4\pi^2 f^2 L}$

Or,  $C = \frac{1}{4 \times (3.14)^2 \times (50)^2 \times 80 \times 10^{-3}}$

$\therefore C = 127 \mu\text{F}$

5.

(a) average value of current of complete cycle is zero

**Explanation:** The average value of alternating current over a complete cycle is zero

6.

(d)  $L/2$

**Explanation:** The resonance frequency is given by

$f_0 = \frac{1}{2\pi\sqrt{LC}}$

When C is changed to 2C,  $f_0$  will remain unchanged, if L is changed to  $L/2$ .

7.

(c) 2 A

**Explanation:** Here,  $N_p = 140$ ;  $N_s = 280$  and  $I_p = 4$  A

$\therefore I_s = I_p \times \frac{N_p}{N_s} = 4 \times \frac{140}{280} = 2\text{A}$

8.

(d) 0.05 J

**Explanation:**  $U = \frac{1}{2} LI^2$

$= \frac{1}{2} \times 100 \times 10^{-3} \times (1)^2 = 0.05 \text{ J}$

9.

(b) 13.3  $\mu\text{F}$

**Explanation:**  $V = 170$  volt,  $f = 60$  Hz,  $i = 0.85$  A

$V = iX_C = i \frac{1}{\omega C} = \frac{i}{2\pi f C}$

Thus, Capacitance required,

$C = \frac{i}{2\pi f V} = \frac{0.85}{2 \times 3.14 \times 60 \times 170} = 13.3 \times 10^{-6} \text{ F} = 13.3 \mu\text{F}$

10.

(c) frequency

**Explanation:** Input and output voltages have same frequency in a transformer.

11. (a) 0.1 A

**Explanation:** Current in the secondary coil is given by,  $i = \frac{V_s}{Z} = \frac{22}{220} = 0.1A$

12.

(d)  $\sqrt{2}$

**Explanation:** Power factor,  $\cos \phi = \frac{R}{Z}$

In first case:

$$Z_1 = \sqrt{R^2 + X_L^2} = \sqrt{R^2 + (3R)^2} = R\sqrt{10}$$

$$\cos \phi_1 = \frac{R}{Z_1} = \frac{R}{R\sqrt{10}} = \frac{1}{\sqrt{10}}$$

In second case:

$$Z_2 = \sqrt{R^2 + (X_L - X_C)^2} = \sqrt{R^2 + (3R - R)^2} = R\sqrt{5}$$

$$\cos \phi_2 = \frac{R}{Z_2} = \frac{R}{R\sqrt{5}} = \frac{1}{\sqrt{5}}$$

The ratio of new to old power factor is

$$\frac{\cos \phi_2}{\cos \phi_1} = \frac{\frac{1}{\sqrt{5}}}{\frac{1}{\sqrt{10}}} = \frac{\sqrt{2}}{1}$$

$$\cos \phi_2 : \cos \phi_1 = \sqrt{2} : 1$$

13. (a) soft iron

**Explanation:** Soft iron provides the best material for the core of a transformer as its permeability ( $\mu$ ) is very high. Its hysteresis curve is of small area and its coercivity is very low.

14. (a) 10  $\Omega$

**Explanation:** 10  $\Omega$

15. (a) 66 V, 210 V

**Explanation:**  $R = 100\Omega$

$$C = 10\mu F$$

$$V = 220 \text{ volt}$$

$$f = 50\text{Hz}$$

$$Z = \sqrt{R^2 + X_C^2}$$

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi fC} = \frac{1}{2 \times 3.14 \times 50 \times 10 \times 10^{-6}} = 318.5\Omega$$

$$Z = \sqrt{(100)^2 + (318.5)^2} = 333.8\Omega$$

Current in circuit,

$$i = \frac{V}{Z} = \frac{220}{333.8} = 0.66A$$

$$\text{Voltage across the resistor, } V_R = iR = 0.66 \times 100 = 66V$$

$$\text{Voltage across the capacitor, } V_C = iX_C = 0.66 \times 318.5 = 210V$$

16.

(c) 90 %

**Explanation:** The efficiency of a transformer

$$\eta = \frac{\text{Output power}}{\text{Input power}} = \frac{V_s I_s}{V_p I_p}$$

$$\text{Here } V_s I_s = 100 \text{ W, } V_p = 220 \text{ V, } I_p = 0.5 \text{ A}$$

$$\therefore \eta = \frac{100}{220 \times 0.5} = 0.90 = 90 \%$$

17.

(d) 400

**Explanation:**  $N_p$  = no. of turns in primary coil = 4000

$N_s$  = no. of turns in secondary coil

$$V_p = \text{input voltage} = 2300 \text{ V}$$

$$V_s = \text{output voltage} = 230 \text{ V}$$

Now,  $\frac{V_s}{V_p} = \frac{N_s}{N_p}$

$$\frac{230}{2300} = \frac{N_s}{4000}$$

Thus,  $N_s = 400$

18. (a) zero

**Explanation:** The voltage across L and C are out of phase with each other. Hence, the voltage across LC-combination is zero.

19.

(c)  $5\sqrt{3}$  V

**Explanation:**  $\varepsilon = \varepsilon_0 \cos 2\pi ft$

$$= 10 \cos\left(2\pi \times 50 \times \frac{1}{600}\right) \text{V}$$

$$= 10 \cos \frac{\pi}{6} = 10 \times \frac{\sqrt{3}}{2} = 5\sqrt{3} \text{ V}$$

20.

(c) Pure resistive circuit

**Explanation:** Since in pure resistive circuit the current and voltage are in phase, the power dissipation is maximum.

21.

(c)  $\frac{1}{400}$  s

**Explanation:**  $I = I_0 \sin 2\pi ft = 100 \sin 200\pi t$

$$\therefore 2f = 200 \text{ or } f = 100 \text{ Hz}$$

$$T = \frac{1}{f} = \frac{1}{100} \text{ s}$$

Time taken by current to rise from zero to peak value

$$= \frac{T}{4} = \frac{1}{4 \times 100} \text{ s} = \frac{1}{400} \text{ s}$$

22.

(d) 311 V

**Explanation:** 311 V

23.

(b)  $90^\circ$

**Explanation:** If only inductor is present in circuit, then  $R = 0$

$$\tan \phi = \frac{X_L}{R} = \frac{X_L}{0} = \infty$$

Hence, phase angle,  $\phi = 90^\circ$

24.

(d) zero

**Explanation:** Since reactive impedance at resonance is zero and we know that,

$$\tan \phi = X_L - \frac{X_C}{Z}$$

$$\text{but } X_L - X_C = 0$$

therefore  $\phi = 0$

25. (a) soft iron

**Explanation:** Soft iron is best because of its high permeability and low hysteresis loss.

26.

(c) first decreases to become zero and then increases

**Explanation:** first decreases to become zero and then increases

27. (a) A.C. voltage

**Explanation:** A transformer changes the magnitude of a.c.

28. (a) there is no wastage of power

**Explanation:** A choke reduces the current in an ac circuit without dissipating any power.

29.

(c) Both  $V_{\text{rms}} = \frac{V_0}{\sqrt{2}}$  and  $V_{\text{rms}} = 0.707 V_0$

**Explanation:**  $V_{\text{rms}} = \frac{V_0}{\sqrt{2}} = 0.707 V_0$

30.

(c) another capacitor should be added in parallel to the first

**Explanation:** Resonant frequency in an L-C-R circuit is given by

$$v_0 = \frac{1}{2\pi\sqrt{LC}}, \quad v_0 \text{ is the frequency and } L \text{ is the inductor and } C \text{ for the capacitor.}$$

If L or C increases, the resonant frequency will reduce.

To increase capacitance, we must connect another capacitor parallel to the first.

31. (a) soft iron

**Explanation:** Soft iron is used for the core of a transformer because of its high permeability and low hysteresis loss.

32. (a) 200 V - 50 Hz

$$\mathbf{Explanation:} \quad \varepsilon_2 = \frac{N_2}{N_1} \cdot \varepsilon_1 = \frac{500}{50} \times 20 = 200 \text{ V}$$

The frequency remains unchanged.

33. (a) 200 V - 50 Hz

$$\mathbf{Explanation:} \quad \varepsilon_s = \frac{N_s}{N} \cdot \varepsilon_p$$

$$= \frac{5000}{500} \times 20 = 200 \text{ V}$$

frequency remains the same.

34.

(c) 161 V

**Explanation:**  $R = 300.0 \Omega$ ,  $X_C = 300.0 \Omega$  and  $X_L = 500.0 \Omega$ ,  $P_{av} = 60W$ 

$$Z = \sqrt{R^2 + (X_L - X_C)^2} = \sqrt{300^2 + (500 - 300)^2} = 100\sqrt{13}\Omega$$

$$P_{av} = V_{rms} \times I_{rms} \times \cos \phi$$

$$\text{Now, } I_{rms} = \frac{V_{rms}}{Z}$$

$$\cos \phi = \frac{R}{Z}$$

$$\text{Thus, } P_{av} = \frac{(V_{rms})^2}{Z} \times \frac{R}{Z} = \frac{(V_{rms})^2 R}{Z^2}$$

$$60 = \frac{(V_{rms})^2 \times 300}{100\sqrt{13} \times 100\sqrt{13}}$$

$$V_{rms} = \sqrt{\frac{60 \times 100 \times 13}{3}} = 161V$$

35.

(d) 146.0  $\Omega$ **Explanation:**  $R = 115\Omega$ 

$$C = 1.25\mu F = 1.25 \times 10^{-6} F$$

$$L = 4.5mH = 4.5 \times 10^{-3} H$$

Resonant angular frequency is given by ,

$$\omega_0 = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{4.5 \times 10^{-3} \times 1.25 \times 10^{-6}}} = \frac{1}{7.5 \times 10^{-5}}$$

$$\text{Given that the angular frequency of the ac source, } \omega = \frac{\omega_0}{2} = \frac{1}{15 \times 10^{-5}} = 6666.6 \text{ rad/s}$$

Thus, Impedance is given by ,

$$Z = \sqrt{R^2 + \left(\frac{1}{\omega C} - \omega L\right)^2} = \sqrt{115^2 + \left[\left(\frac{1}{6666.6 \times 1.25 \times 10^{-6}}\right) - (6666.6 \times 4.5 \times 10^{-3})\right]^2}$$

$$Z = 146\Omega$$

36. (a) 0.1 J

**Explanation:** Energy stored in the coil is

$$E = \frac{1}{2} Li^2$$

$$L = 50mH = 50 \times 10^{-3}$$

$$i = 2A$$

$$\text{Thus, } E = \frac{1}{2} \times 50 \times 10^{-3} \times 2 \times 2 = 0.1 J$$

37.

(b) L is large and R is small

**Explanation:** L is large and R is small

38.

(c) Power

**Explanation:** Energy losses be zero in transformers hence power remains constant in step down and step up transformer also.

39.

(b) 2000 W

**Explanation:** When the frequency of the supply equals the natural frequency of the circuit,

$$X_L = X_C$$

In this case, impedance  $Z = R$

Average power,

$$P_{av} = V_{rms} \times i_{rms} \times \cos \phi = V_{rms} \times \frac{V_{rms}}{Z} \times \frac{R}{Z}$$

As,  $Z = R$

$$P_{av} = \frac{(V_{rms})^2}{R} = \frac{200 \times 200}{20} = 2000W$$

40.

(b) 25 V

**Explanation:** The resultant voltage in the LCR series circuit is calculated as,

$$V = \sqrt{V_R^2 + (V_C \sim V_L)^2}$$

Here, all alphabets are in their usual meanings.

$$V_R = 20 \text{ V}, V_C = 30 \text{ V and } V_L = 15 \text{ V}$$

$$\text{So, } V = \sqrt{(20)^2 + (30 \sim 15)^2}$$

$$V = \sqrt{400 + 225} = \sqrt{625}$$

$$V = 25 \text{ V}$$

41.

(c) 5.5 V

$$\text{Explanation: } V_s = \frac{N_s}{N_p} \times V_p = \frac{100}{2000} \times 110 = 5.5 \text{ V}$$

42. (a) admittance

**Explanation:** The reciprocal of the impedance of an a.c. the circuit is called admittance.

43.

(b)  $-X_g$

**Explanation:** For maximum power to be delivered from the generator (or internal reactance  $X_g$ ) to the load (of reactance,  $X_L$ )

$$\Rightarrow X_L + X_g = 0 \text{ (the total reactance must vanish)}$$

$$\Rightarrow X_L = -X_g$$

thus the maximum power from generator to the load  $X_L$  is given by  $= -X_g$

44. (a) 3 V

$$\text{Explanation: } \varepsilon_2 = \frac{N_2}{N_1} \cdot \varepsilon_1 = \frac{2}{1} \times 1.5 = 3 \text{ V}$$

45.

(b) 189.7  $\Omega$

$$\text{Explanation: } X_L = 2\pi fL = 2\pi \times 50 \times 0.5 = 157.08\Omega$$

$$X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi \times 50 \times 10^{-5}} = 318.31\Omega$$

$$X_C - X_L = 161.23\Omega$$

$$Z = \sqrt{R^2 + (X_C - X_L)^2} = \sqrt{100^2 + (161.23)^2}$$

$$= \sqrt{35995.07} = 189.72 \Omega$$

46. (a) 3 A

$$\text{Explanation: } \eta = \frac{\text{Output}}{\text{Input}}$$

$$\frac{80}{100} = \frac{20 \times 120}{1000 \times I}$$

$$I = \frac{20 \times 120 \times 100}{1000 \times 80} = 3A$$

47.

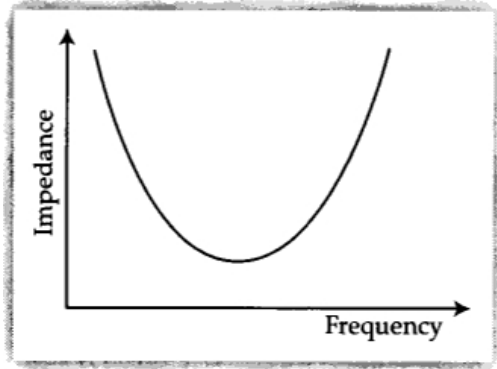
(b)  $\frac{V_0}{\sqrt{2}}$

$$\text{Explanation: } \frac{V_0}{\sqrt{2}}$$

48.

(b) decreases at first, becomes minimum and then increases

**Explanation:** The frequency vs. Impedance graph of a series LCR circuit is as follows:



With increase in frequency, the impedance decreases at first, becomes minimum and then increases.

49.

(d) 1.1 V

**Explanation:**  $\frac{V_s}{V_p} = \frac{N_s}{N_p} \Rightarrow \frac{V_s}{220} = \frac{40000}{200}$

$\therefore V_s = 44000 \text{ V}$

P.D. per turn =  $\frac{44000}{40000} = 1.1 \text{ V}$

50. (a) frequency

**Explanation:** Transformer does not change the frequency of the applied AC.

51.

(d)  $22 \times 10^3 \text{ cal}$

**Explanation:**  $H = \frac{\epsilon_{rms}^2 t}{RJ} = \frac{\epsilon_0^2 t}{2RJ} = \frac{(220)^2 \times 7 \times 60}{2 \times 110 \times 4.2}$

$= 22 \times 10^3 \text{ cal}$

52.

(b) 5.0 ampere

**Explanation:**  $\eta = \frac{V_s I_s}{V_p I_p}$

$\therefore I_p = \frac{V_s I_s}{\eta V_p} = \frac{440 \times 2}{0.80 \times 220} = 5 \text{ A}$

53.

(c) eddy current

**Explanation:** Lamination increases the resistance and hence reduced the eddy current.

54.

(d)  $\frac{X}{4}$

**Explanation:** The capacitive reactance X is given by,

$X = \frac{1}{2\pi fC}$

Let new reactance after doubling frequency and capacitance is  $X'$ .

So,  $X' = \frac{1}{2\pi(2f)(2C)}$

$\Rightarrow X' = \frac{1}{4(2\pi fC)}$

$\Rightarrow X' = \frac{X}{4}$

55.

(d)  $\sqrt{R^2 + (X_L - X_C)^2}$

**Explanation:**  $\sqrt{R^2 + (X_L - X_C)^2}$

56.

(b)  $3.2 \times 10^{-3} \text{ A}, 0.16 \text{ A}$

**Explanation:**  $\frac{I_1}{I_2} = \frac{3.2 \times 10^{-3}}{0.16} = \frac{1}{50} = \frac{10}{500} = \frac{N_2}{N_1}$

57.

(c) 120 V

**Explanation:** Flux linked with the primary coil,

$$\phi = \phi_0 + 4t$$

Voltage across primary,

$$V_p = \frac{d\phi}{dt} = 0 + 4 \times 1 = 4 \text{ V}$$

Voltage across secondary,

$$V_s = \frac{N_s}{N_p} \cdot V_p = \frac{1500}{50} \times 4 = 120 \text{ V}$$

58.

(d)  $\frac{1}{4}$

**Explanation:**  $\omega = \frac{1}{\sqrt{LC}}$

For,  $\omega = \text{constant} \rightarrow \sqrt{LC} = \text{constant}$

Therefore, C is inversely proportional to L

So, if C is made 4C then L should be reduced to  $\frac{1}{4}$  to keep  $\omega$  constant.

59.

(c) only L

**Explanation:** When a circuit inductance only, then the current lags behind the voltage by the phase difference of  $\pi/2$ .

60.

(c) 10 W

**Explanation:** Let P = actual power used

W = power specified = 40 W

$V_A$  = Applied voltage = 100 V

$V_S$  = Specified voltage = 200 V

Now,

$$P = \left(\frac{V_A}{V_S}\right)^2 W$$

$$P = \left(\frac{100}{200}\right)^2 \times 40 = 10 \text{ W}$$

61.

(c) lags behind the applied emf by an angle  $\frac{\pi}{2}$

**Explanation:** lags behind the applied emf by an angle  $\frac{\pi}{2}$

62. (a) Current

**Explanation:** Current increases in a step-down transformer.

63.

(b) lags voltage in phase by  $\frac{\pi}{2}$ .

**Explanation:** lags voltage in phase by  $\frac{\pi}{2}$ .

64. (a) 90%

**Explanation:**  $\eta = \frac{\text{output power}}{\text{input power}} = \frac{V_s I_s}{V_p I_p} \times 100 = \frac{100}{220 \times 0.5} \times 100 = 90\%$

65.

(d) 50 amp

**Explanation:**  $\frac{N_s}{N_p} = \frac{i_p}{i_s} = \frac{V_s}{V_p} = r$

Given that  $\frac{N_p}{N_s} = \frac{1}{25}$

$i_s = 2$  amp

Thus,  $\frac{25}{1} = \frac{i_p}{2}$

$i_p = 50$  amp

66.

(d) mutual induction

**Explanation:** A transformer works on the principle of mutual induction.

67. (a) 84.8 V

**Explanation:**  $V_{\text{rms}} = 0.707 V_0 = 0.707 \times 120 \text{ V} = 84.8 \text{ V}$

68.

(c)  $\frac{1}{\sqrt{2}A}$

**Explanation:** According to the problem output/secondary voltage  $V_s = 24\text{V}$

Power associated with secondary  $P_s = 12\text{W}$

$$I_s = \frac{P_s}{V_s} = \frac{12}{24} = 0.5\text{A}$$

The amplitude of the current in the secondary winding

$$I_0 = I_s \sqrt{2}$$

$$= (0.5) (1.414) = 0.707 = \frac{1}{\sqrt{2}}\text{A}$$

thus the value of peak current is given by  $= 0.707\text{A} = \frac{1}{\sqrt{2}}\text{A}$

69.

(b) 50.0 V

**Explanation:**  $V_R = 30\text{V}$ ,  $V_C = 90\text{V}$ ,  $V_L = 50\text{V}$

$$V = \sqrt{(V_C - V_L)^2 + V_R^2} = \sqrt{(90 - 50)^2 + 30^2} = \sqrt{40^2 + 30^2}$$

$V = 50 \text{ volt}$

70.

(d) the meter reads not  $v$  but  $\langle v^2 \rangle$  and is calibrated to read  $\sqrt{\langle v^2 \rangle}$

**Explanation:** the meter reads not  $v$  but  $\langle v^2 \rangle$ . The voltmeter connected to AC mains calibrated to read rms value  $\sqrt{\langle v^2 \rangle}$

71.

(c) step-down transformer with turn ratio 2 : 1

**Explanation:** The ratio between the number of primary turns to the number of secondary turns being called the “turns ratio” or “transformer ratio”.

$$\text{Thus, } \frac{N_p}{N_s} = \frac{V_p}{V_s} \left( = \frac{\text{input}}{\text{output}} \right)$$

$$\frac{N_p}{N_s} = \frac{220}{110} = \frac{2}{1}$$

Turn ratio is  $N_p : N_s = 2 : 1$

As  $N_p > N_s$ , hence it is a step down transformer.

72.

(d) 0.124 H

**Explanation:**  $R = 48\Omega$

$f = 80\text{Hz}$

$$\phi = 53^\circ$$

$$\text{Now, } \omega = 2\pi f = 2 \times 3.14 \times 80$$

In series LR circuit,

$$\tan \phi = \frac{\omega L}{R}$$

$$\tan 53^\circ = \frac{2 \times 3.14 \times 80 \times L}{48}$$

$$\frac{4}{3} = \frac{2 \times 3.14 \times 80 \times L}{48}$$

Thus,  $L = 0.124 \text{ H}$

73.

(b)  $5\sqrt{\frac{3}{2}} \text{ A}$

**Explanation:** According to the problem, frequency,  $v = 50 \text{ Hz}$ ,  $I_{\text{rms}} = 5\text{A}$

$$t = \frac{1}{300} \text{ s}$$

$$I_0 = \text{Peak value of } \sqrt{2} (I_{\text{rms}}) = 5\sqrt{2}$$

$$= 5\sqrt{2}\text{A}$$

$$\text{From, } I = I_0 \sin \omega t = 5\sqrt{2} \sin 2\pi vt = 5\sqrt{2} \sin 2\pi \times 50 \times \frac{1}{300}$$

$$= 5\sqrt{2} \sin \frac{\pi}{3} = 5\sqrt{2} \times \frac{\sqrt{3}}{2} = 5\sqrt{\frac{3}{2}}\text{A}$$

74. (a)  $146 \Omega$

**Explanation:**  $R = 115 \Omega$

$$C = 1.25 \mu F = 1.25 \times 10^{-6} F$$

$$L = 4.5 mH = 4.5 \times 10^{-3} H$$

Resonant angular frequency,

$$\omega_0 = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{4.5 \times 10^{-3} \times 1.25 \times 10^{-6}}} = \frac{1}{7.5 \times 10^{-5}}$$

Given that the angular frequency of the ac source,  $\omega = 2\omega_0 = \frac{2}{7.5 \times 10^{-5}} = 26666.6 \text{ rad/s}$

impedance,

$$Z = \sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2} = \sqrt{115^2 + \left[(26666.6 \times 4.5 \times 10^{-3}) - \left(\frac{1}{26666.6 \times 1.25 \times 10^{-6}}\right)\right]^2}$$

$$Z = 146 \Omega$$

75.

(b) 220 V, 50 Hz

**Explanation:** In India, we use electricity at 220 volt and 50 hertz.